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Numerical Modeling of the Thomson Ring in Stationary Levitation Using FEM-Electrical Network and Newton-Raphson

Modelación numérica del anillo de Thomson en levitación estacionaria usando circuitos eléctricos, MEF y Newton-Raphson

Guzmán Juan

*Departamento de Energía
Universidad Autónoma Metropolitana (UAM)
Unidad Azcapotzalco
E-mail: maestro_juan_rafael@hotmail.com*

González-Montañez Felipe de Jesús

*Departamento de Energía
Universidad Autónoma Metropolitana (UAM)
Unidad Azcapotzalco
E-mail: fjgm@correo.azc.uam.mx*

Escarela-Pérez Rafael

*Departamento de Energía
Universidad Autónoma Metropolitana (UAM)
Unidad Azcapotzalco
E-mail: r.escarela@ieee.org*

Olivares-Galván Juan Carlos

*Departamento de Energía
Universidad Autónoma Metropolitana (UAM)
Unidad Azcapotzalco
E-mails: jolivare_1999@yahoo.com*

Jiménez-Mondragon Victor Manuel

*Departamento de Energía
Universidad Autónoma Metropolitana (UAM)
Unidad Azcapotzalco
E-mail: vmjm1986@gmail.com*

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Abstract

There are a lot of applications of the Thomson ring: levitation of superconductor materials, power interrupters (used as actuator) and elimination of electric arcs. Therefore, it is important the numerical modeling of Thomson ring. The aim of this work is to model the stationary levitation of the Thomson ring. This Thomson ring consists of a copper coil with ferromagnetic core and an aluminum ring threaded in the core. The coil is fed by a cosine voltage to ensure that the aluminum ring is in a stationary levitated position. In this situation, the state of the electromagnetic field is stable and can be used the phasor equations of the electromagnetic field. These equations are discretized using the Galerkin method in the Lagrange base space (*finite element method*, FEM). These equations are solved using the COMSOL software. A methodology is also described (which uses the Newton-Raphson method) that obtains the separation between coil and aluminum ring. The numerical solutions of this separation are compared with experimental data. The conclusion is that the magnetic coupling of the aluminum ring on the coil can be neglected if the source voltage is high.

Keywords:

- Thomson ring
- levitation
- stationary
- modeling
- FEM

Resumen

Existen una gran cantidad de aplicaciones del anillo de Thomson: levitación de materiales superconductores, interruptores de potencia (usados como actuadores) y eliminación de arcos eléctricos. Por lo tanto, es importante la modelación del anillo de Thomson. El objetivo de este trabajo es modelar la levitación estacionaria del anillo de Thomson. Este anillo de Thomson consiste de una bobina de cobre con núcleo ferromagnético y un anillo de aluminio enhebrado en el núcleo. La bobina se alimenta por un voltaje cosenoidal para asegura el anillo de aluminio en una posición de levitación estacionaria. En esta situación, el campo electromagnético se puede considerar estable y se pueden emplear las ecuaciones fasoriales del campo electromagnético. Estas ecuaciones se discretizan usando el método de Galerkin en el espacio base de Lagrange (método de elementos finitos, FEM). Estas ecuaciones discretizadas se resuelven usando el código COMSOL. Además, se describe una metodología con la cual se puede obtener la separación entre la bobina y el anillo de aluminio. Esta metodología usa el método de Newton-Raphson. Las soluciones numéricas de esta separación se comparan con datos experimentales. Se concluye que el acoplamiento magnético entre el anillo de aluminio sobre la bobina se puede despre- ciar si el voltaje de alimentación es alto.

Descriptores:

- anillo de Thomson
- levitación
- estacionaria
- modelación
- MEF

Introduction

In the electric industry is important to have electric systems of immediate breaking and safe. Some of these electric systems consist of power switchers, which use the Thomson ring (Alferov *et al.*, 2008; Meyer and Rufer, 2006). Other systems utilize the Thomson ring as actuator to eliminate the electric arcs (Li *et al.*, 2010). Other applications of the Thomson ring consist in the levitation of superconductor materials (Patitsas, 2011). Therefore, it is important the numerical modeling of the Thomson ring. The Thomson ring consists of a coil with ferromagnetic core on which an aluminum ring levitates. The coil is fed by a cosine voltage.

The modeling of the electromagnetic field of any electric device (as the Thomson ring) requires of the knowledge of the current density. However, this knowledge cannot be known a priori. It is known a priori the power source voltage instead of current density. In the literature, several methods (Belforte *et al.*, 1985; Bissal *et al.*, 2010; Konrad, 1982; Lombard and Meunier, 1992, 1993; Meunier *et al.*, 1988; Piriou and Razek, 1989) have been developed to calculate the electromagnetic field if the power source voltage is supplied: integro-differential method (Konrad, 1982); direct methods (Belforte *et al.*, 1985; Meunier *et al.*, 1988; Piriou and Razek, 1989); and methods that use electric networks equations (Barry and Casey, 1999; Bissal *et al.*, 2010; Lombard and Meunier, 1992, 1993). In this work is supposed that the power source voltage is known and the current density is calculated using electric networks equations.

Several studies have analyzed the mathematical and physics models of the Thomson ring. In the work of Bissal *et al.* (2010) is modeled the dynamic behavior of the Thomson ring, which consist of a coil without ferromagnetic core. In this work, the coil is fed by a capacitor. Barry and Casey (1999) obtained analytical solutions of the force acting on the aluminum ring in a stationary levitated position. In the work of Li *et al.* (2010) is analyzed the dynamic characteristics of the Thomson ring used as actuator to eliminate the electric arcs. In the work of Patitsas (2011) is developed a new modality of Thomson ring. This modality consisted in keeping the stable levitation of a superconductor sphere immerse in a magnetic field supplied by a coil.

The aim of this work is to analyze the Thomson ring when the aluminum ring is a stationary levitated position. This situation is reached if the coil is fed by a cosine voltage. In the stationary levitation, the state of the electromagnetic field is stable and can be used the phasor equations of the electromagnetic field. These equations are discretized using the Galerkin method. These discretized equations are solved using the COMSOL software (COMSOL, 2008). It is described the methodology (which uses the Newton-Raphson method) that obtains the separation between the coil and the aluminum ring in stationary levitation (mechanical equilibrium). Also, the separation obtained with this methodology is compared with the experimental data for different values of the power source voltage. It is concluded that the magnetic coupling of the aluminum ring on the coil can be neglected if the source voltage is high.

Experimental setup

The Thomson ring used in this work consists of a coil with ferromagnetic core; where an aluminum ring is threaded on the core, as shown in Figure 1. The ferromagnetic core consists in a solid cylinder that is collocated vertically, as is illustrated in Figure 1. In this figure, Z_s represents the distance between the coil and the aluminum ring.

The coil is made of copper wire and consists of 1140 turns (see, Table 1). This coil is fed by a cosine voltage given by

$$V = V_0 \cos(\omega t) \quad (1)$$

where, V_0 is the amplitude; $\omega = 2\pi f$ is the angular frequency (f being the natural frequency), as shown in Table 1. The electric and magnetic characteristics of the materials used in the Thomson ring are indicated in Table 1. The ferromagnetic core is iron whose relativity permeability is taken from the data base of COMSOL (2008).

In order to take advantage of axial symmetry, the Thomson ring is represented by means of axisymmetric geometry as depicted in Figure 2. In this Figure, a cylinder coordinate system is chosen so that the r -axis represents the horizontal axis, the z -axis represents the vertical axis. The dimensions of the aluminum ring are: interior radius of 0.031 m, exterior radius of 0.0365 m and height

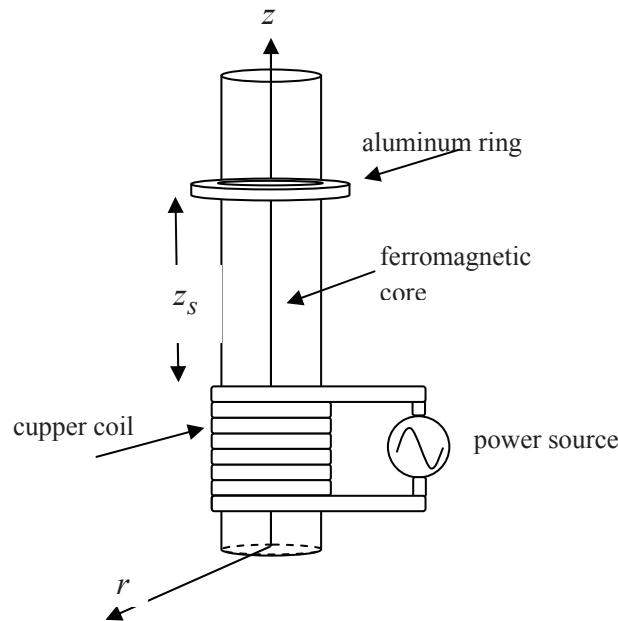


Figure 1. Thomson ring setup

Table 1. Parameters used in the Thomson ring

	Aluminum ring	Copper coil	Ferromagnetic core
Relativity permittivity (ϵ_r)	1	1	1
Relativity permeability (μ_r)	1	1	4000
Electric conductivity (σ)	3.77×10^7 S/m	5.99×10^7 S/m	1.12×10^7 S/m
Coil turn (N)		1140 turns	
Natural frequency (f)		60 Hz	

of 0.018 m as illustrated in Figure 2. In this figure, Z_s is the separation distance between aluminum ring and copper coil.

The copper coil forms a toroid with dimensions: interior radius of 0.025 m, exterior radius of 0.039 m, and height of 0.075 m, as shown in Figure 2. The distance between base of ferromagnetic core and base of copper coil is 0.025 m. The copper coil is threaded on a ferromagnetic cylinder (ferromagnetic core). The ferromagnetic core has a radius of 0.0235 m and height of 0.41 m, as depicted in Figure 2.

Solution methodology

Electromagnetic field equations

In this section the equations that describe the electromagnetic field in the Thomson ring are presented. The magnetic field $\vec{B} = \nabla \times \vec{A}$ (\vec{A} being the magnetic vector potential) satisfies the Ampere-Maxwell equation

$$\nabla \times (\nu \nabla \times \vec{A}) = \vec{J} + \frac{\partial \vec{D}}{\partial t} \quad (2)$$

where, ν is the relativity, \vec{J} is the current density; and $\vec{D} = \epsilon \vec{E}$ (ϵ being the permittivity) is the electric density. The second term in the Eq. (2) represents the displacement current, which can be dropped if the frequency of the power source is small; in this case, the Eq. (2) is given by

$$\nabla \times (\nu \nabla \times \vec{A}) = \vec{J} \quad (3)$$

The current density \vec{J} in this equation depends of the type of region (copper coil, aluminum ring, air or ferromagnetic core) and is given by:

1) Air and ferromagnetic core region

The current density in air and ferromagnetic core regions is $\vec{J} = \vec{0}$; therefore

$$\nabla \times (\nabla \times \vec{A}) = \vec{0}.$$

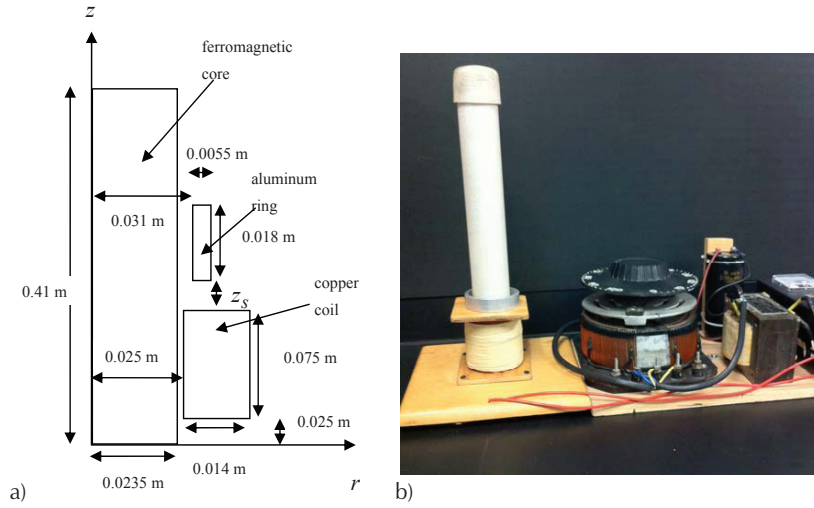


Figure 2. a) axisymmetric representation of the Thomson ring, b) experimental setup

2) Aluminum ring region

The current density $\vec{J} = \sigma_r \vec{E}$ (being σ_r the electric conductivity of the aluminum ring) is found using the Faraday law

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} \quad (5)$$

Solving this equation for the vector potential \vec{A}

$$\vec{E} = -\frac{\partial \vec{A}}{\partial t} \quad (6)$$

It is observed that this equation does not contain the term of the scalar electric potential gradient (ΔV) due to that there is not a power source in the aluminum region. Substituting Eq. (6) in $\vec{J} = \sigma_r \vec{E}$

$$\vec{J} = -\sigma_r \frac{\partial \vec{A}}{\partial t} \quad (7)$$

Substituting Eq. (6) in Eq. (3)

$$\nabla \times (\nu \nabla \times \vec{A}) + \sigma_r \frac{\partial \vec{A}}{\partial t} = \vec{0} \quad (8)$$

3) Copper coil region

The region of the copper coil is modeled as a region that contains N turns where each turn carries the same cur-

rent i_c . In this case, the current density J is uniform with value

$$J = \frac{Ni_c}{S_c} \quad (9)$$

where, S_c is the cross section area of the copper coil region. Substituting Eq. (9) in Eq. (3)

$$\nabla \times (\nu \nabla \times \vec{A}) = \frac{Ni_c}{S_c} \hat{I} \quad (10)$$

where, \hat{I} is a unit vector pointed in direction of the current density.

Electrical network equations

If the current is known, the solution of the Eq. (10) can be realized. However, this current cannot be known a priori. We know a priori the voltage V between the terminals of the coil. An additional equation is required. This equation is obtained using the Kirchhoff voltage law

$$V = Ri_c + \frac{d\Phi}{dt} \quad (11)$$

where, R is the resistance, Φ is the magnetic flux that cross all the turns of the coil. The resistance is given by

$$R = \frac{NL}{\sigma_c S_c} \quad (12)$$

where, σ_c is the electric conductivity of the coil and L is the length of all the turns of the coil. The magnetic flux is given by

$$\Phi = \int_{S_c} \vec{B} \cdot d\vec{S} \quad (13)$$

where, the surface S_c comprises all the surfaces of the turns of the coil. Using the fact $\vec{B} = \nabla \times \vec{A}$ and the Stokes theorem in Eq. (13) we obtain

$$\Phi = \int_C \vec{A} \cdot d\vec{r} \quad (14)$$

where, the trajectory C comprises all the turns of the coil. Substituting Eq. (14) in Eq. (11)

$$V = Ri_c + \frac{d}{dt} \int_C \vec{A} \cdot d\vec{r} \quad (15)$$

Phasor equations

The current in the copper coil is cosine to ensure that the aluminum ring stays in a stationary levitated position. In this situation, the state of the electromagnetic field is stable and the equations of the electromagnetic field can be given in phasor form. In phasor notation, the operator d/dt becomes $i\omega$ in Eqs. (4), (8) and (10):

air and ferromagnetic core regions

$$\nabla \times (\nabla \times \vec{A}) = \vec{0} \quad (16)$$

aluminum ring region

$$\nabla \times (\nu \nabla \times \vec{A}) + \sigma_r i\omega \vec{A} = \vec{0} \quad (17)$$

copper coil region

$$\nabla \times (\nu \nabla \times \vec{A}) = \frac{Ni_c}{S_b} \hat{r} \quad (18)$$

where, \vec{A} and i_c are phasors of the potential \vec{A} and the current i_c respectively.

The phasor equation of the electrical network equation Eq. (15) is

$$V = Ri_c + i\omega \int_C \vec{A} \cdot d\vec{r} \quad (19)$$

where, V is the phasor of the voltage V .

Boundary conditions

It is observed that Eq. (3) is a second order partial differential equation for the magnetic vector potential \vec{A} . The solution of this partial differential equation requires boundary conditions for the vector potential \vec{A} . The boundary of the solution domain is chosen so that the vector potential can be dropped (magnetic insulation). The magnetic insulation condition is expressed as

$$\vec{A} = \vec{0} \text{ on } \Gamma \quad (20)$$

where, Γ is the boundary of solution domain. In phasor notation, the condition of magnetic insulation is

$$\vec{A} = \vec{0} \text{ on } \Gamma \quad (21)$$

Discretization

Using the Galerkin method (Hoole, 1989; Lombard and Meunier, 1992, 1993), Eqs. (16)-(19) can be discretized:

air and ferromagnetic core regions

$$[S][A'] = [0] \quad (22)$$

aluminum ring region

$$[S][A'] + i\omega[G][A'] = 0 \quad (23)$$

copper coil region

$$[S][A'] = i_c[C] \quad (24)$$

electrical network equation

$$V = Ri\omega i_c + i\omega[B]^T[A'] \quad (25)$$

With

$$A' = rA \quad (26)$$

where N represents the number of nodes. The matrices and vectors are defined as

$$[S]_{ij}(N \times N) = \int_{S_d} \frac{2\pi v}{r} \nabla \beta_i \nabla \beta_j dS \quad (27)$$

$$[G]_{ij}(N \times N) = \int_{S_d} \frac{2\pi \sigma_r}{r} \beta_i \beta_j dS \quad (28)$$

$$[C]_i(N \times 1) = -\frac{2\pi N}{S_c} \int_{S_d} \beta_i dS \quad (29)$$

$$[B]_i(N \times 1) = \int_C \beta_i dr \quad (30)$$

where, the vector potential A is expanded in the base function β_i : $A = \sum \beta_i A_i$. The surface S_d is the surface of the solution domain.

Mechanical equilibrium

The voltage is a cosine in order to maintain the aluminum ring in a stationary levitated position. This stationary levitation is obtained when the mechanical equilibrium is reached; this is, the Lorentz force averaged in a cycle, f_{zav} equals the gravity force f_g . Using the complex notation, the Lorentz force f_{zav} (Barry and Casey, 1999; Hayt and Buck, 2006) is given by

$$f_{zav} = \frac{1}{2} \int_{V_r} \vec{J} \times \vec{B}^* dV \quad (31)$$

with

$$\vec{B}^* = \text{complex}(\vec{B}) \quad (32)$$

where, \vec{B} and \vec{J} are the phasors of magnetic density \vec{B} and current density \vec{J} , respectively. The factor 1/2 in Eq. (31) is due to that the Lorentz force period is half of

the magnetic field period (Barry and Casey, 1999). Figure 3 shows the flowchart of the obtaining of the average Lorentz force. The steps of this methodology are:

- 1) Calculate the phasor potential using the phasor equations (Eqs. 22-25) along with boundary condition of magnetic insulation $\vec{A} \cdot \hat{n} = 0$ on Γ (see Eq. 20).
- 2) Determine the phasor magnetic density $\vec{B} = \nabla \times \vec{A}$ and phasor current density $\vec{J} = i\omega \sigma_r \vec{A}$ (see Eq. 6) in the aluminum ring region.
- 3) Calculate the average Lorentz force $f_{zav} = \frac{1}{2} \int_{V_r} \vec{J} \times \vec{B}^* dV$ (see Eq. 31).

The space distribution of the electromagnetic field depends of the separation s_z between the aluminum ring and the copper coil. Therefore, the average Lorentz force f_{zav} is a function of the separation ($f_z = f_z(s_z)$). In order to reach the stationary levitation of the aluminum ring, the average Lorentz force f_{zav} equals to the gravity force f_g .

$$f_{zav}(z_s) = f_g \quad (33)$$

where, z_s' is the separation in stationary levitation and represents the root of Eq. (33). It is observed that Eq. (33) is a transcendental equation. The root of this transcendental equation can be found using a variant of the Newton-Raphson method: secant method (Arfken and Weber, 2005). The convergence of Newton-Raphson is guaranteed due to that the average Lorentz

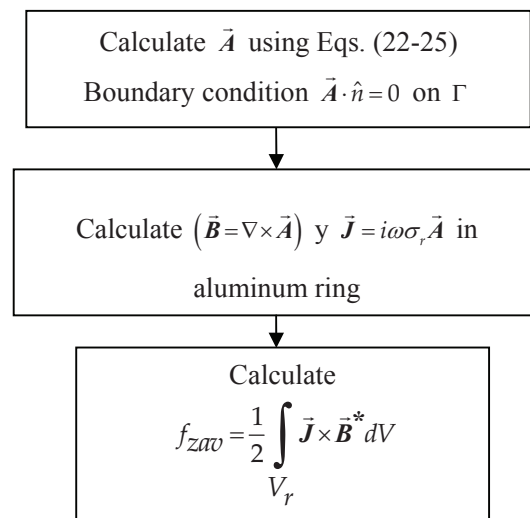


Figure 3. Flowchart of the obtaining of f_{zav}

force $f_{zav}(z_s)$ is a function decreasing of the separation z_s (see Figure 5). The secant method is defined by the recurrence relation

$$z_{n+1} = z_n - \frac{z_n - z_{n+1}}{f_{zav}(z_n) - f_{zav}(z_{n+1})} (f_{zav}(z_n) - f_g) \quad (34)$$

Experimental validation

In this section we compared the numerical and experimental results for the separation in stationary levitation z'_s as a function of the voltage amplitude in rms,

$V_{rms} = \frac{V_0}{\sqrt{2}}$. The experimental setup was described in

the second section. The numerical results are obtained using the proposed methodology in the section above. Figure 4 shows the separation z'_s as function of the voltage amplitude V_{rms} for both experimental and numerical results. The discrepancy between the theoretical and experimental data is at most 12%. This difference can be due to the fact that the numerical modeling does not take into account the temperature effect in the electric conductivity σ .

Results and discussion

In this section some results obtained by the proposed modeling are studied. The average Lorentz force is examined as a function of the separation distance; the ratio between coil current and ring current, and the spatial distribution of the magnetic field.

Figure 5 depicts the average Lorentz force f_{zav} as function of the separation z_s for a representative voltage amplitude $V_{rms} = 120$ V. It is observed that the Lorentz force is a decreasing function of the distance z_s . This guarantees the convergence of the Newton-Raphson

method due to that the derivative $\frac{df_{zav}}{dz_s}$ is negative.

Figure 6 shows the spatial distribution of the radial component B_{r0} of the magnetic density amplitude, for a representative voltage amplitude $V_{rms} = 120$ V in state of stationary levitation ($z'_s = 0.057$ m). It also presents the positions of the ferromagnetic core, copper coil and aluminum ring. This Figure 6 shows that the radial component is higher in regions close to the core, coil and ring edges. In contrast, the radial component B_{r0} presents small values in positions far away from above edges.

The total current in the ring i_r is realized by means of

$$i_r = \int_{ring} \vec{J} \cdot d\vec{S}; \text{ while the total current in the region of}$$

the coil is Ni_c . In Figure 7 is shown the ratio $\frac{i_r}{Ni_c}$ as

function of voltage amplitude V_{rms} in stationary levitation. It is observed that the highest value ($i_r / Ni_c = 0.47$) occurs in $V_{rms} = 43.4$ V corresponding to a separation $z'_s = 0$. The ratio i_r / Ni_c decreases if the voltage amplitude V_{rms} increases. Also, in a first order approach, the magnetic field originated by any system is proportional to the current of this system. Therefore, the magnetic coupling of the ring on the coil can be neglected for high values of voltage amplitude.

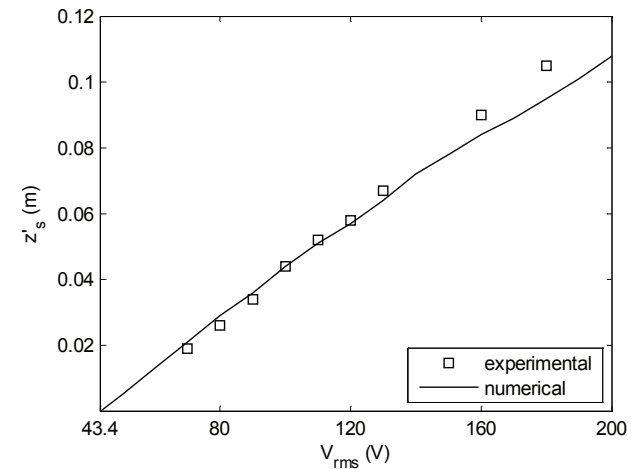


Figure 4. z'_s vs V_0 for theoretical and experimental data

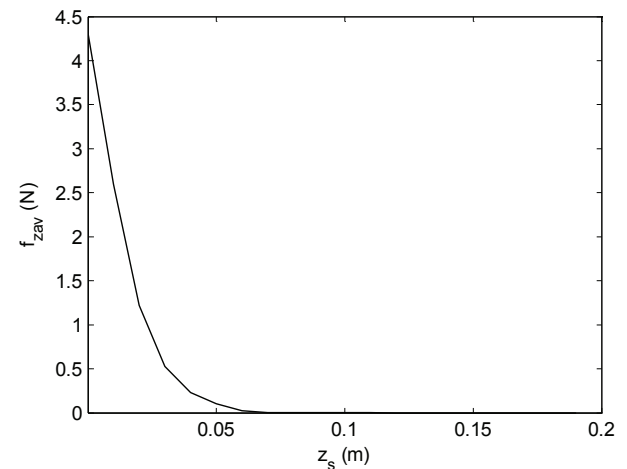
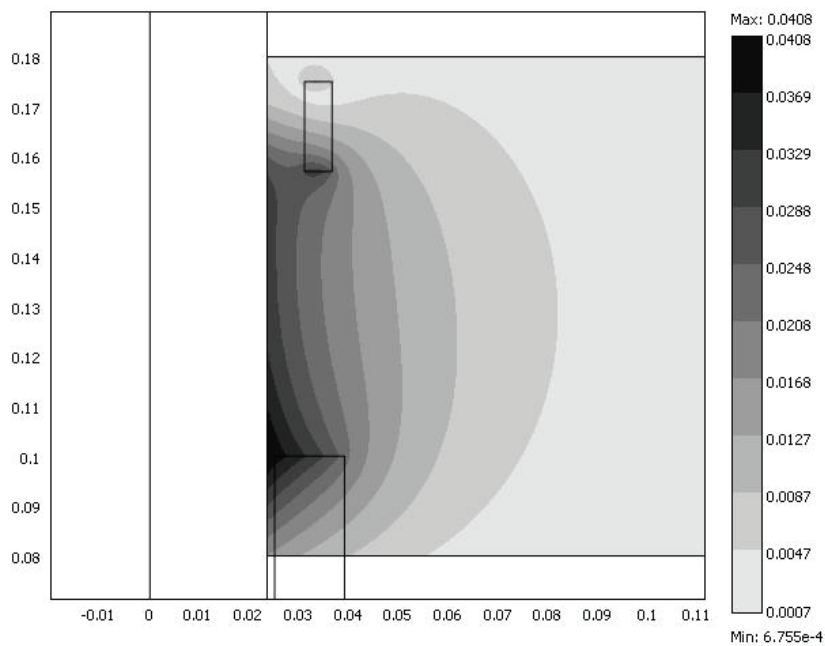
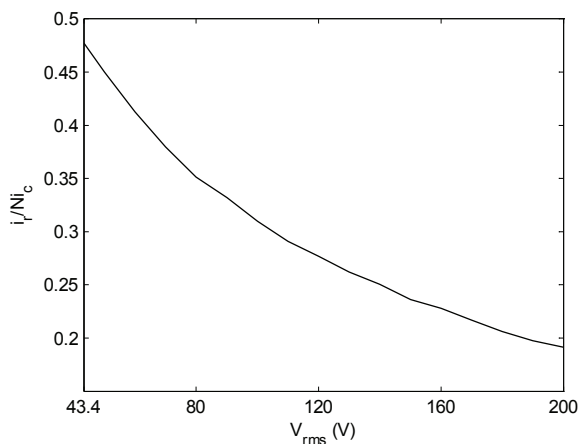


Figure 5. Average Lorentz force f_{zav} as a function of the distance z_s


 Figure 6. Spatial distribution of the radial component $B_{r0}(T)$

 Figure 7. $\frac{i_r}{N i_c}$ as function of V_{rms}

Conclusions

The aim of this work was to present a numerical modeling based upon the use of the Galerkin method to simulate the electromagnetic field of the Thomson ring. Also, this modeling is capable of simulating numerically the separation between aluminum ring and copper coil in situation of stationary levitation (the average Lorentz force equals gravity force). This calculation of the separation uses the Newton-Raphson method.

The proposed modeling was validated comparing theoretical and experimental results. The compared re-

sults were the separation between the aluminum ring and the copper coil (in stationary levitation) for different voltage amplitudes.

It is concluded that the magnetic coupling of the aluminum ring on the coil can be neglected if the source voltage is high. Therefore, the coil current can be modeled without taking into account the coupling ring-coil. This means that the coil current is found using a RL (resistance-inductance) circuit; where, the resistance and inductance are parameter of the coil.

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About the authors

Juan Guzmán. Obtained Ph.D. in Energy Engineering from the Universidad Nacional Autónoma de México, México City, Mexico, in 2008. He is currently with the área de ingeniería energética y electromagnética, Departamento de Energía, UAM, Azcapotzalco, México.

Felipe de Jesús González-Montañez. He received the M.Sc. degree in electrical engineering from the Centro de Investigación y de Estudios Avanzados del IPN, México City, Mexico, in 2011. His research interests include the modeling and control of electrical machines.

Rafael Escarela-Pérez. He obtained his B.Sc. in electrical engineering from Universidad Autónoma Metropolitana, Mexico City in 1992 and his Ph.D. from Imperial College, London in 1996. He is interested in the modeling of electrical machines.

Juan Carlos Olivares-Galván. He received the Ph.D. degree in electrical engineering from CINVESTAV, Guadalajara, Mexico, in 2003. His main research interests are related to the experimental and numerical analysis of electromagnetic devices.

Victor Manuel Jiménez-Mondragon. He received the M.Sc. degree in electrical engineering from the Universidad Nacional Autónoma de México, México City, Mexico, in 2012. He is interested in the modeling of electrical machines.